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ParisTech

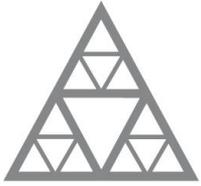
**1) Impacts of small scale rainfall variability in urban areas: a case study with 2D/1D hydrological model in a multifractal framework (presentation from UDM 2012 Conference)**

**2) Comparison between radar and rain gauge estimates (preliminary results)**

**A. Gires, A. Giangola-Murzyn, I. Tchiguirinskaia,  
D. Schertzer, S. Lovejoy**

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# Impacts of small scale rainfall variability in urban areas: a case study with 2D/1D hydrological model in a multifractal framework

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Chair “Hydrology for Resilient Cities” (sponsored by Véolia)



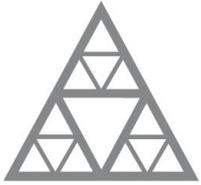
(EU FP 7)



(EU INTER-REG NEW)



# Introduction



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**Basic features of hydrological processes at stake in urban hydrology flooding (rainfall, surface runoff, sewer flow, and sub-surface flow):**

- **Non linear**
- **Different characteristic spatial and temporal scales**

**Numerous studies suggest that rainfall variability, which is extreme over wide ranges of spatial and temporal scales, has a significant impact in hydrology and moreover in urban hydrology (greater coeff. of imper. And shorter response time)**

→ **What is the impact of small scale (< 1 km x 5 min, usually unmeasured) rainfall variability in urban hydrology ?**

→ **What should be the spatial resolution of the model used to take it into account ?**

**A case study :**

- **Kodak Catchment (1.44 km<sup>2</sup> urban near Paris)**
- **Two models : a fully distributed one and a semi distributed one**
- **One rainfall event : 9<sup>th</sup> February, 2009**



# The Multi-Hydro model

## Overall description:

- Multi-hydro is a numerical platform developed at LEESU (v1, El Tabach et al, 2008, v2, A. Giangola-Murzyn et al., 2012) in the framework of SMARTesT. It is currently in a validation and demonstration (Heywood site, Manchester; Villecresnes site, Val-de-Marne) phase.

- It is a core that makes interact different modules, each representing a portion of the water cycle in urban hydrology.

(see Giangola-Murzyn et al. paper at this conference)

## Main goals:

- taking into account small scales → fully distributed model
- physically based model (no calibration)
- easily transportable → a conversion module to generate inputs from available GIS data
- open access software packages to benefit from the feedback of a large community and frequent update.

# The Multi-Hydro model

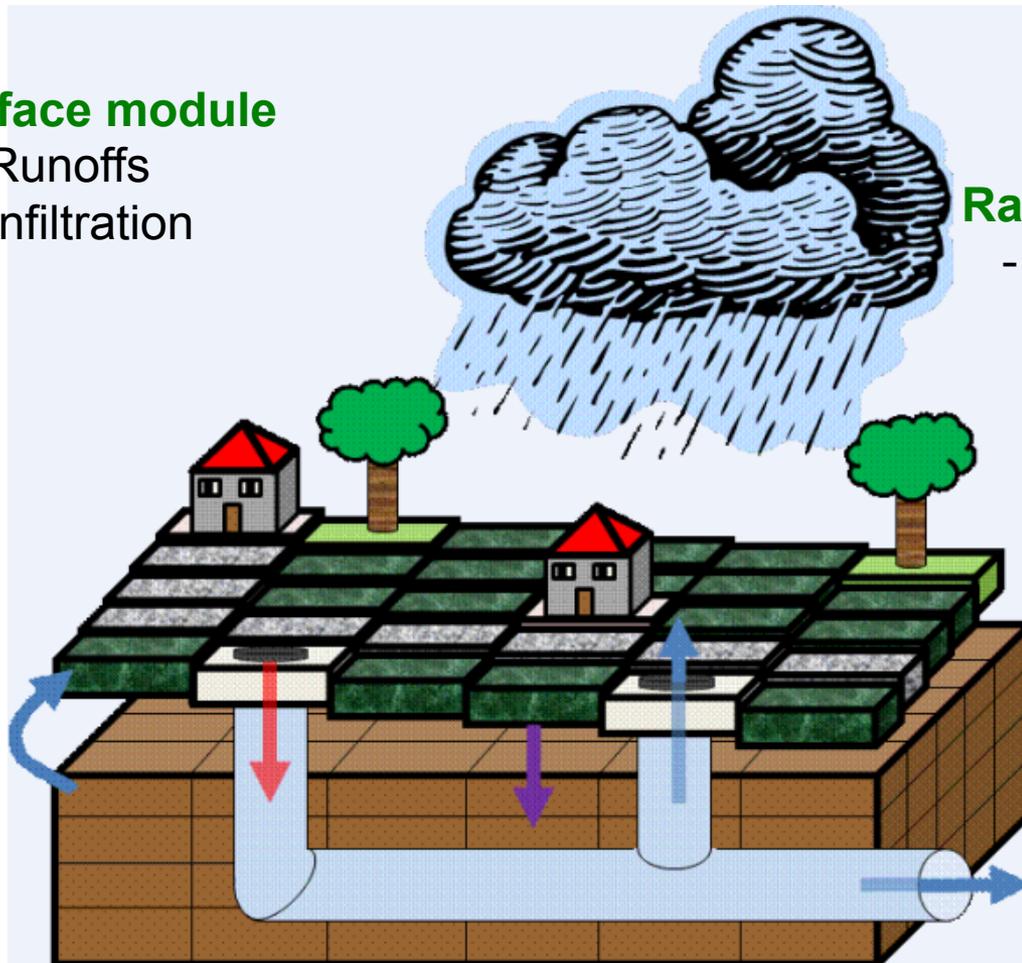
## Urban area physical processes modeled in Multi-Hydro

### Surface module

- Runoffs
- Infiltration

### Rainfall module

- Spatio-temporal rainfall



### Soil module

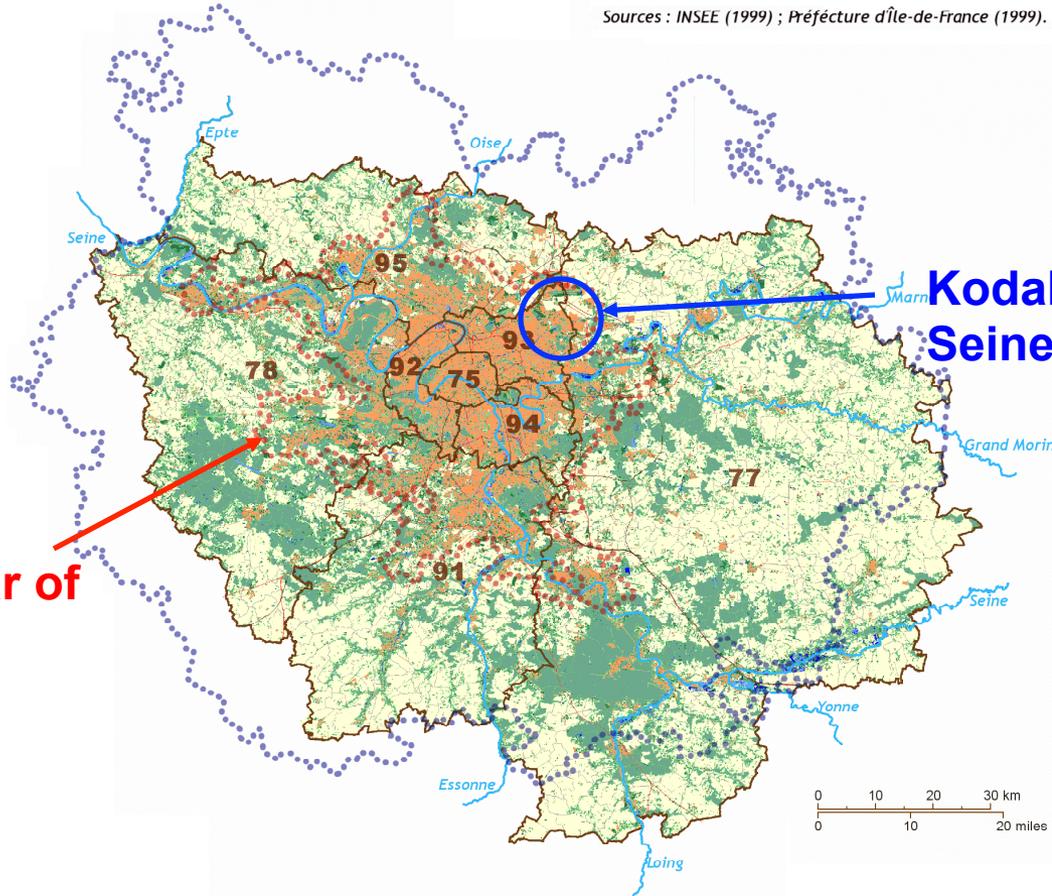
- Vertical flow in the non-saturated area
- Saturation during a rainfall event

### Drainage module

- Sewer flow  
(free surface, and loaded)
- Overflow

# Kodak catchment

Sources : INSEE (1999) ; Préfecture d'Île-de-France (1999).



**Kodak catchment, in Seine-Saint-Denis**

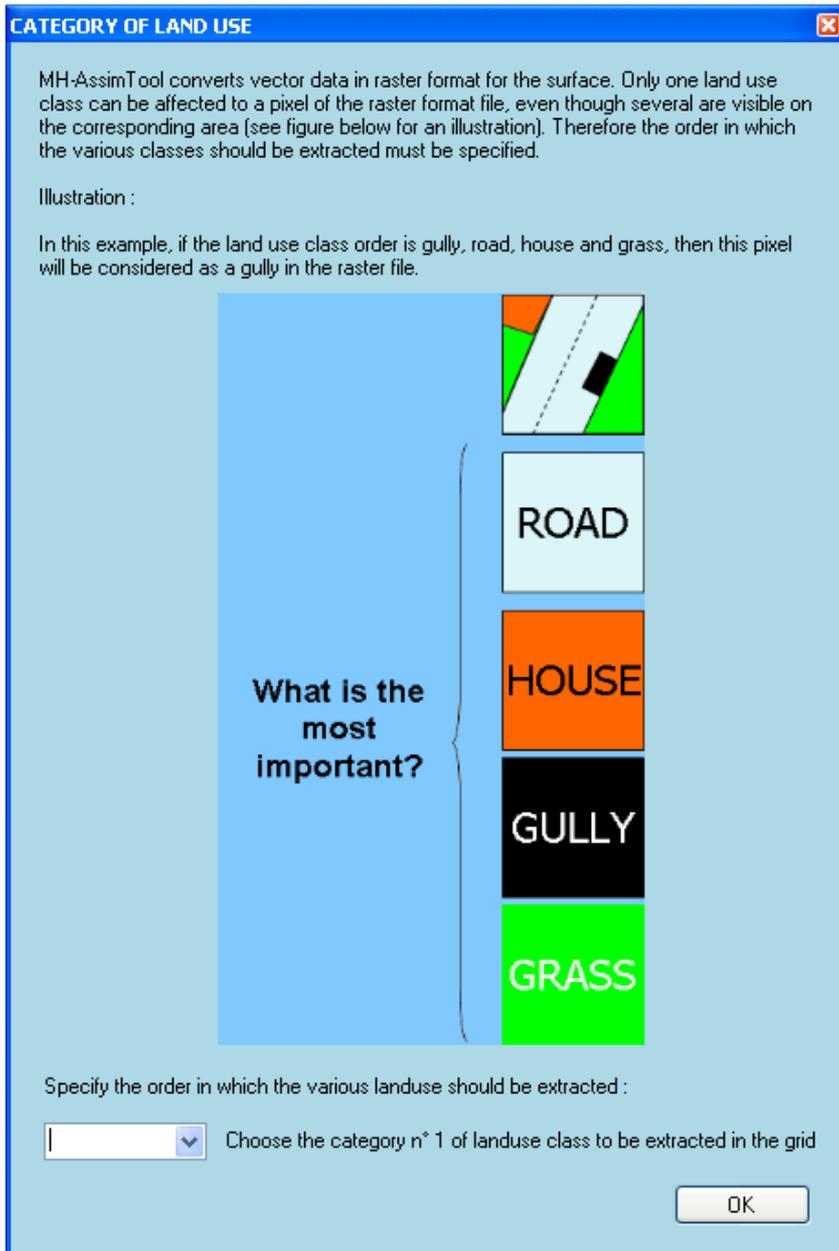
**C band radar of Trappes**

- |   |                              |                          |                          |
|---|------------------------------|--------------------------|--------------------------|
| Paris statistical urban area            | built-up area                | 75 - Paris               | <i>grande couronne :</i> |
| Paris statistical metropolitan area     | wooded area                  | <i>petite couronne :</i> | 77 - Seine-et-Marne      |
| département of the Île-de-France région | agricultural and unused area | 92 - Hauts-de-Seine      | 78 - Yvelines            |
|   |                              | 93 - Seine-Saint-Denis   | 91 - Essonne             |
|   |                              | 94 - Val-de-Marne        | 95 - Val-d'Oise          |

# Kodak catchment



- 1.44 km<sup>2</sup>
- Known for regular overflow
- Project to build a storm water storage basin



*Snapshot of MH AssimTool*

## Multi-Hydro resolution

### Raster data

→ Only one land use class per pixel ...

# Multi-Hydro resolution



# Multi-Hydro resolution



# Multi-Hydro resolution



# Multi-Hydro resolution



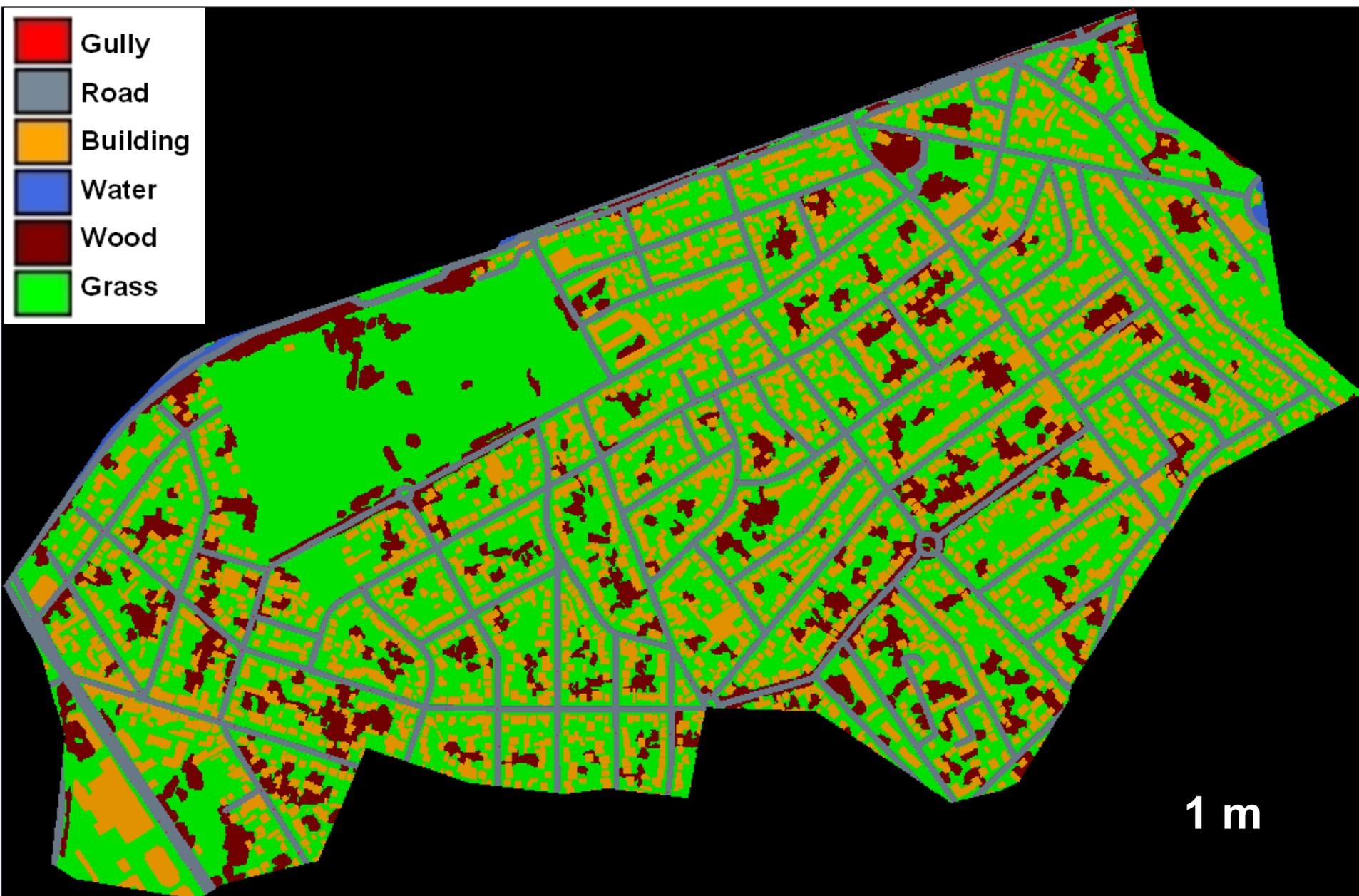
# Multi-Hydro resolution



# Multi-Hydro resolution



# Multi-Hydro resolution



# Multi-Hydro resolution

Example of hydrological consequences:

Size of pixel (m)	% of impervious area
20	87
15	83
10	77
5	63
3	53
2	47
1	40

How to explain these figures with a unique notion ?

# Multi-Hydro resolution

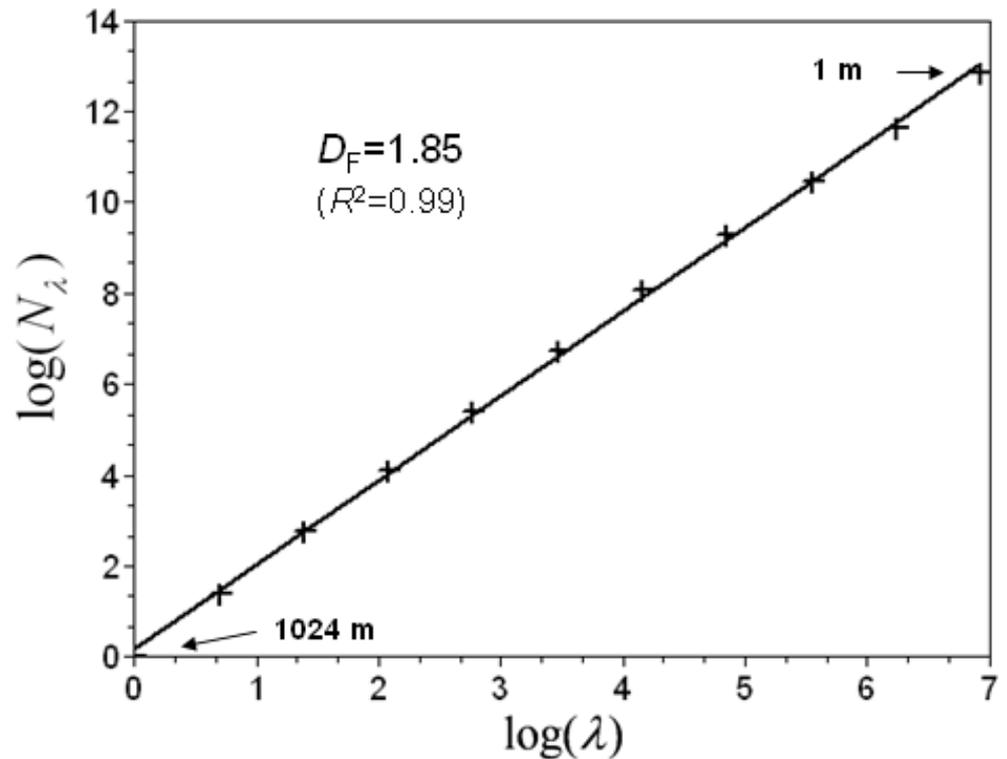
Fractal dimension of the impervious area :

Notion of fractal dimension  
of a set A:

$N_\lambda$  = number of boxes of size  
 $l$  needed to cover the set A  
of outer scale  $L$

$$N_\lambda \approx \lambda^{D_F}$$

$$\text{Resolution} = \lambda = \frac{L}{l}$$



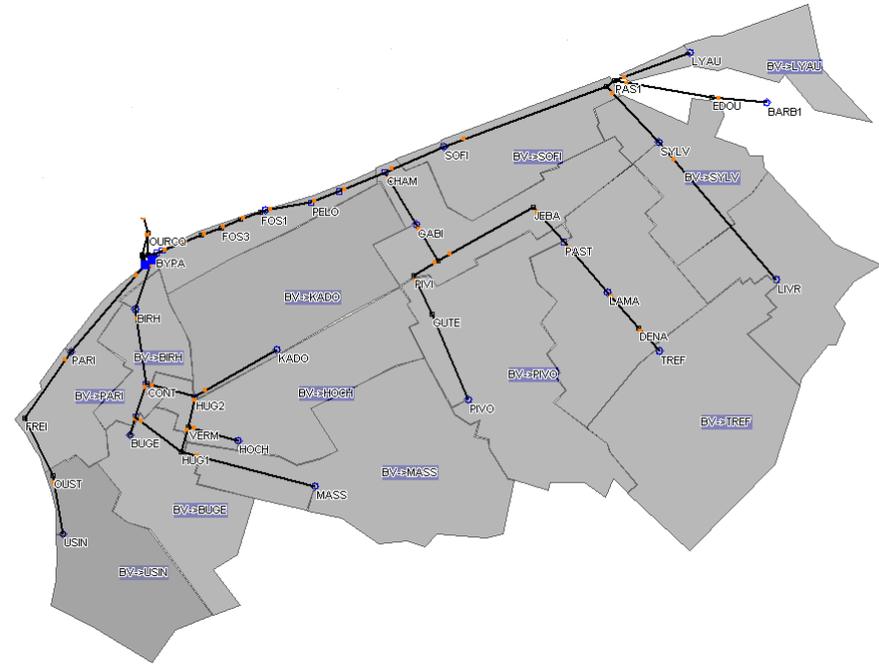
Fractal tools which are commonly  
used in geophysics can also be  
helpful in urban environment.

# Kodak catchment

Multi-Hydro : 10 m resolution



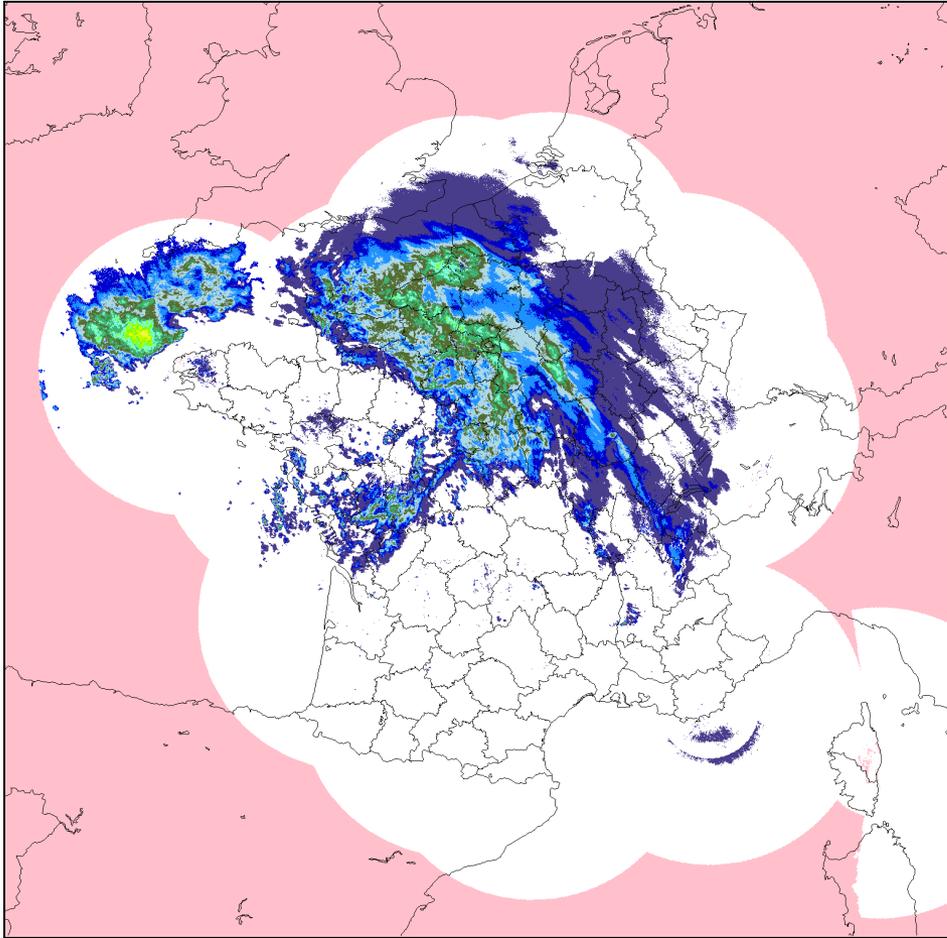
Semi-distributed 1D model



- Modelled with semi-distributed 1D model Canoe (lumped model for each sub-catchment and Saint-Venant equations in the links)
- 16 sub-catchments (considered homogeneous) with size ranging from 4 to 14.5 ha
- Calibrated by DEA 93

# Rainfall event of February 9<sup>th</sup> 2009

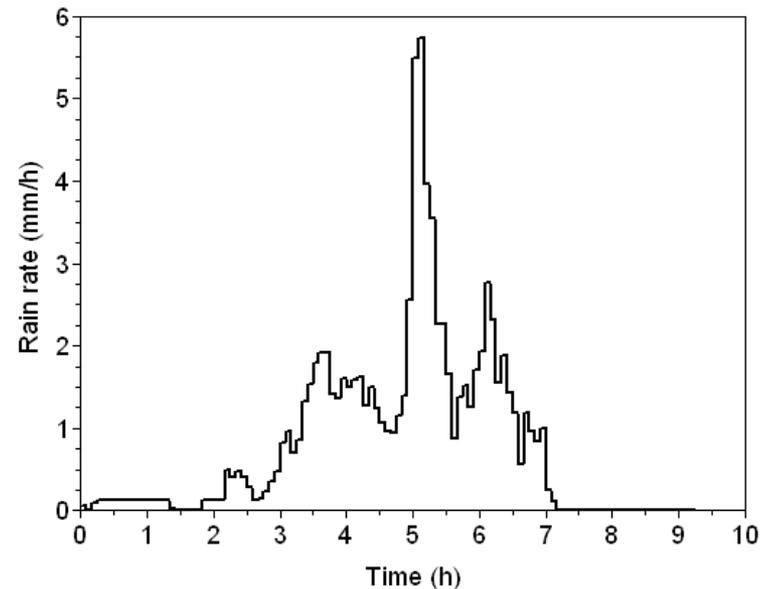
Data : Météo-France radar mosaic



*Météo-France radar mosaic,  
provided by Météo-France*

Resolution :  
1 km \* 1 km \* 5 min

*Time evolution of the rain rate  
for the studied catchment*

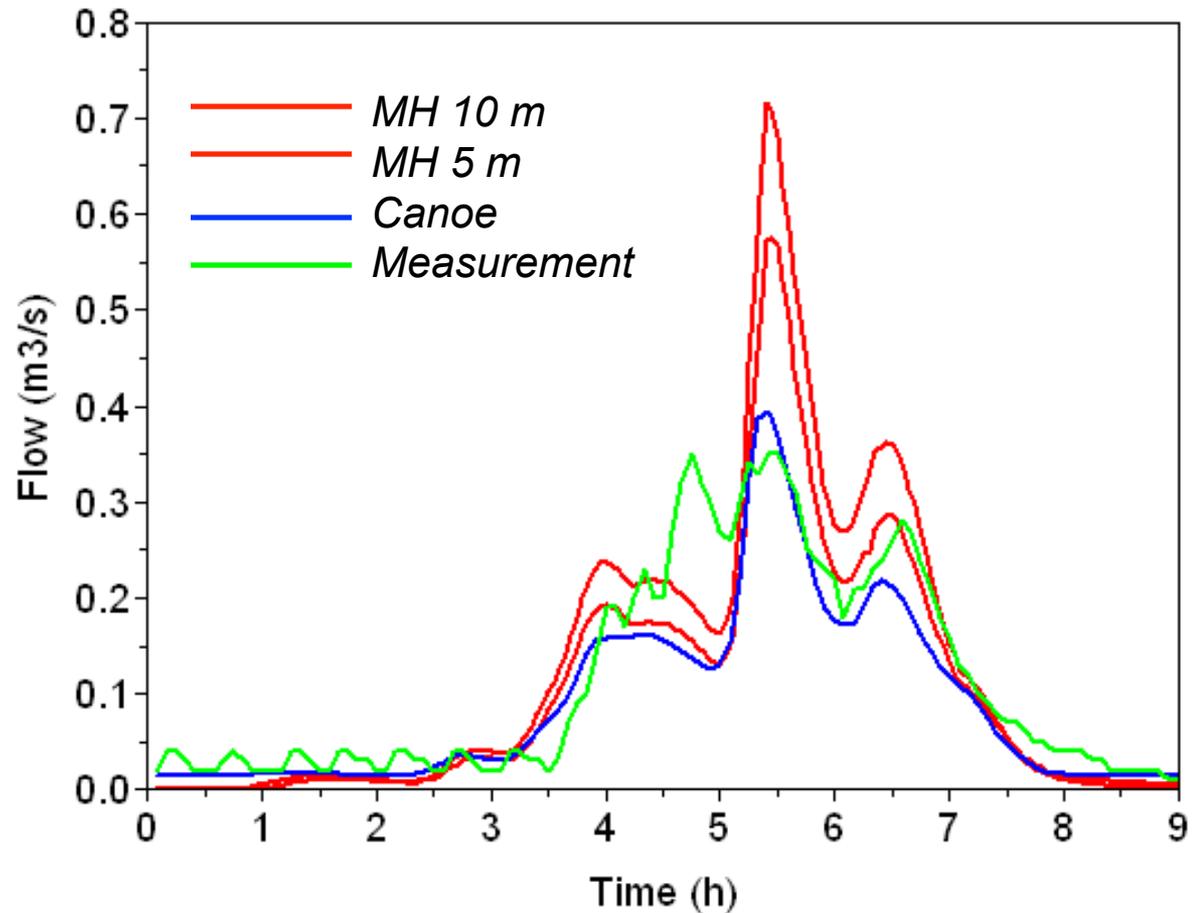


# Comparison of the simulated flow with raw radar data

**For the  
measurement  
point :**

*Nash-Sutcliff*

- MH 10 m : 0.40
- MH 5m : 0.68
- Canoe : 0.78



- Rather similar patterns
- Significant differences in the peak flow
- Data quality ?

# Quantifying the uncertainty associated with small scale rainfall variability

## Methodology : stochastic ensemble approach

### (i) Generation of an ensemble of realistic downscaled rainfall fields :

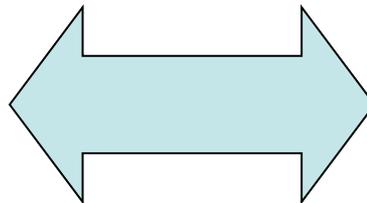
- Multifractal analysis of rainfall data
- Downscaling with the help of discrete universal multifractals cascades

### (ii) Simulation of the corresponding ensembles of hydrographs :

- Use of operational hydrological/hydraulic urban models

### (iii) Analysis of the ensembles :

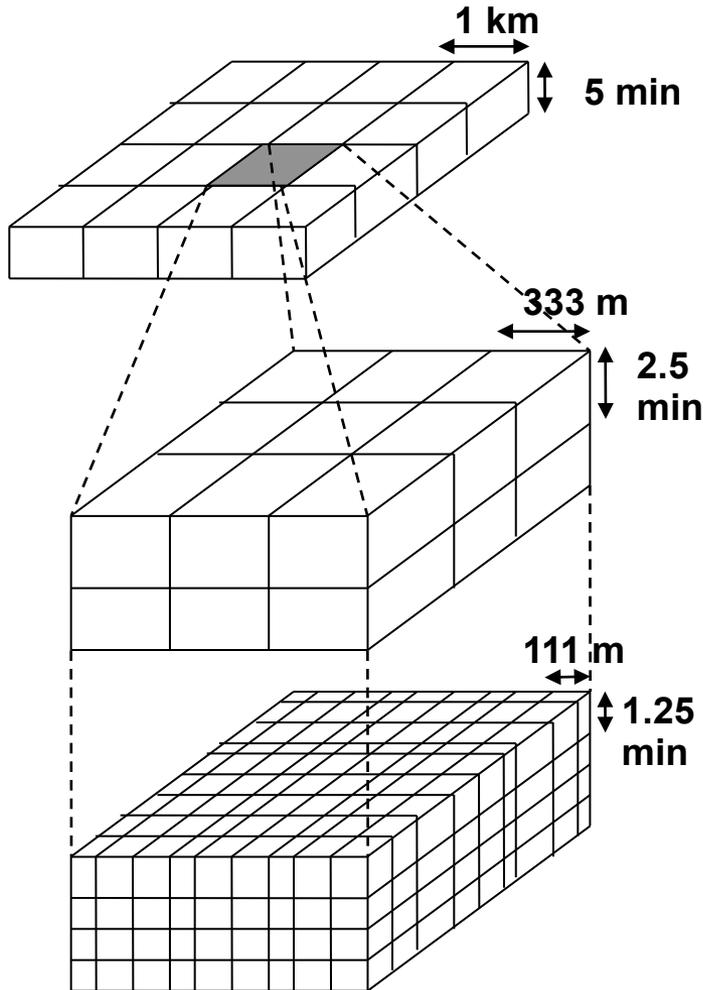
Variability among  
the 100 samples



Uncertainty due to the  
unknown high resolution  
rainfall variability

# Quantifying the uncertainty associated with small scale rainfall variability

## Rainfall downscaling technique



**Measured or  
deterministically nowcasted**

Multifractal analysis → two relevant parameters of the cascade process

**Stochastic spatio-temporal  
downscaling for each pixel**

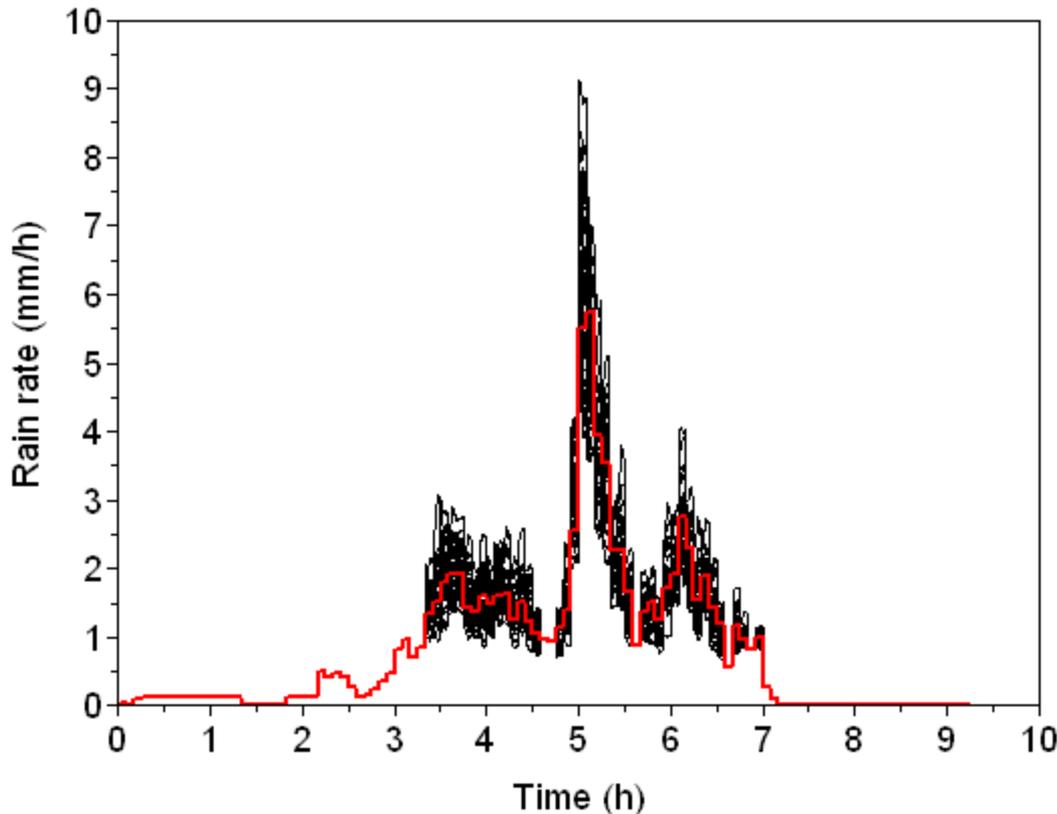
Performed with the help of discrete  
Universal Multifractal cascades

**Two more cascade steps... → 11 m x 19 s**

# Quantifying the uncertainty associated with small scale rainfall variability

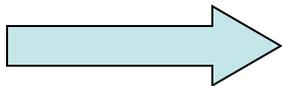
## Rainfall downscaling technique

*Temporal evolution of the avg rain rate over the studied area*



**Total rainfall amount :**

- Raw radar : 7.34 mm
- Simulated ensemble :  $7.37 \pm 0.21$  mm (CV=2.9%)

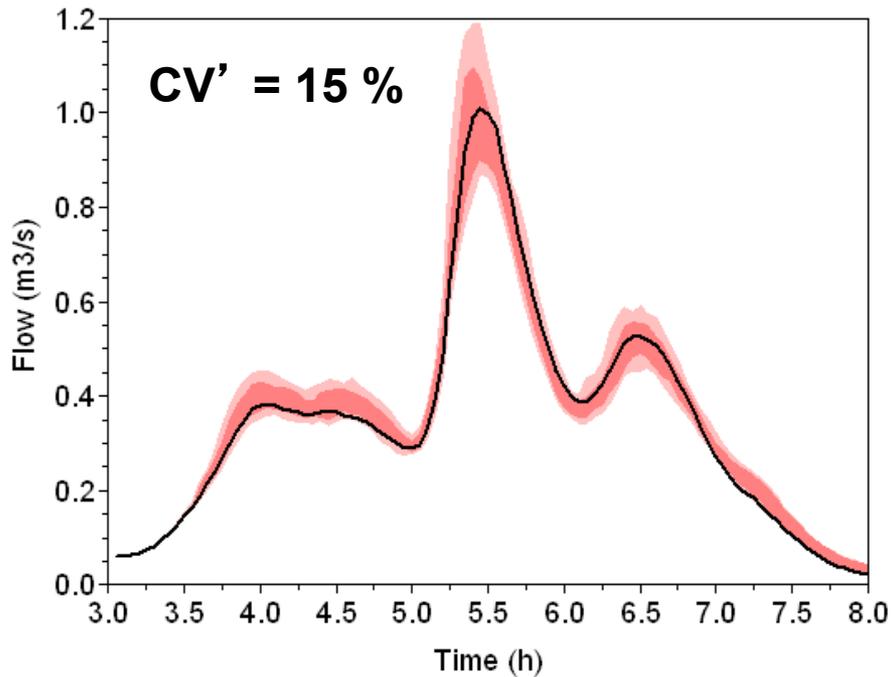


**Potential hydrological effects are due to disparities of spatio-temporal distribution, not total amount.**

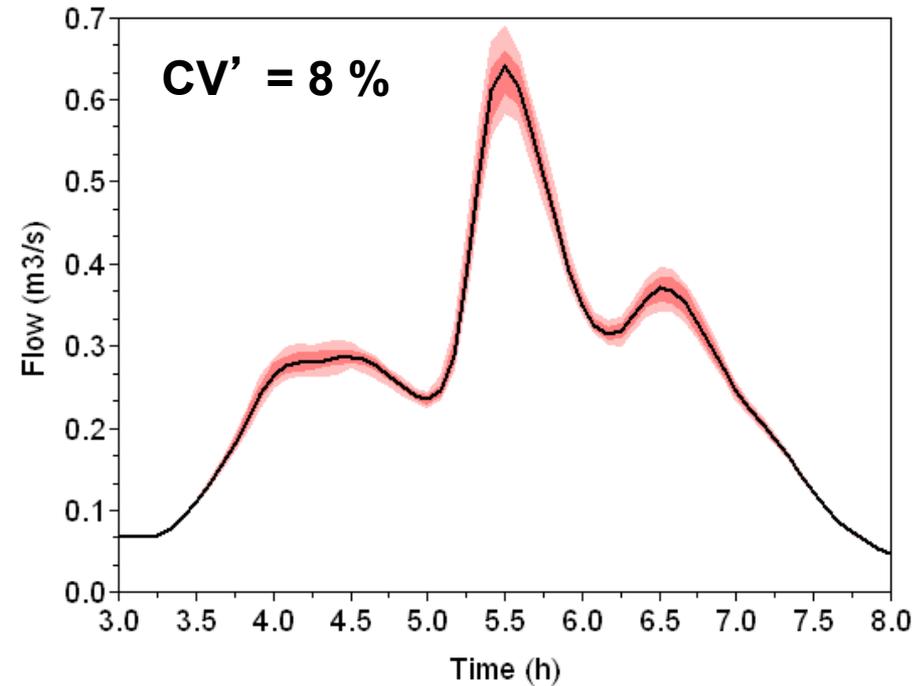
# Quantifying the uncertainty associated with small scale rainfall variability

## Uncertainty on the simulated flow for the outlet

Multi-Hydro 10m



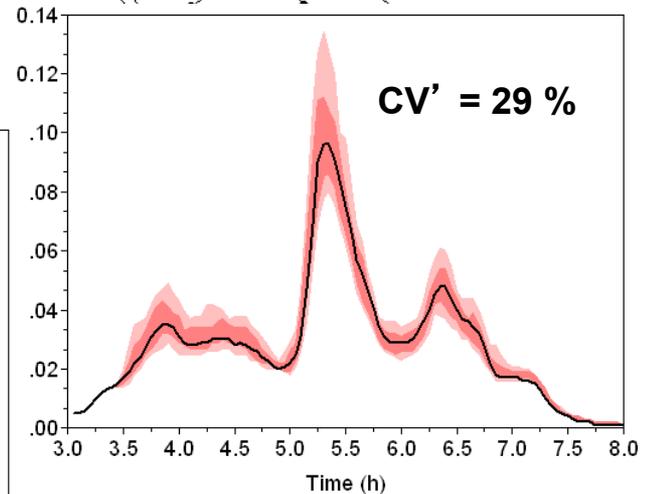
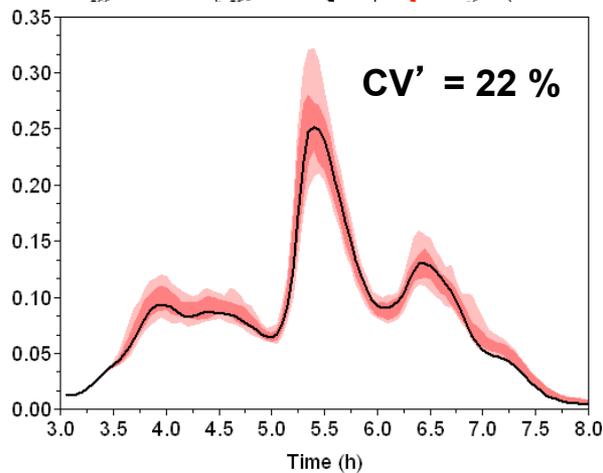
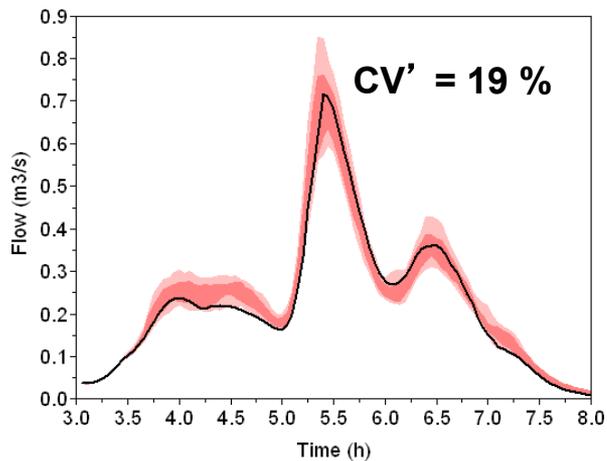
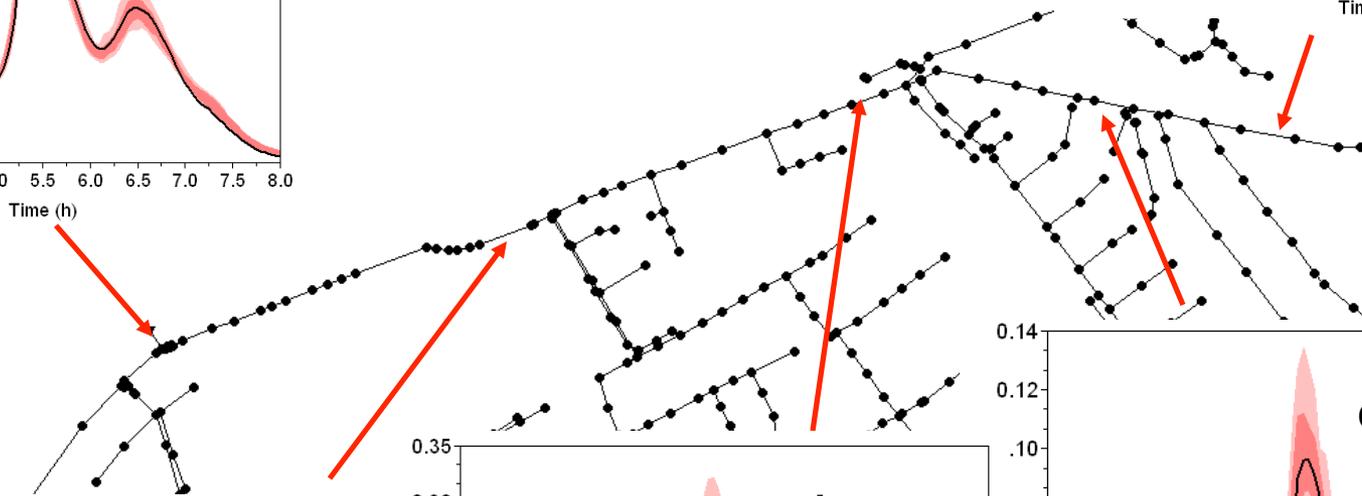
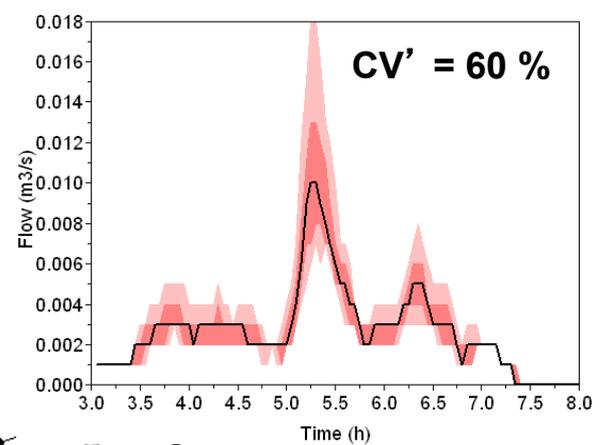
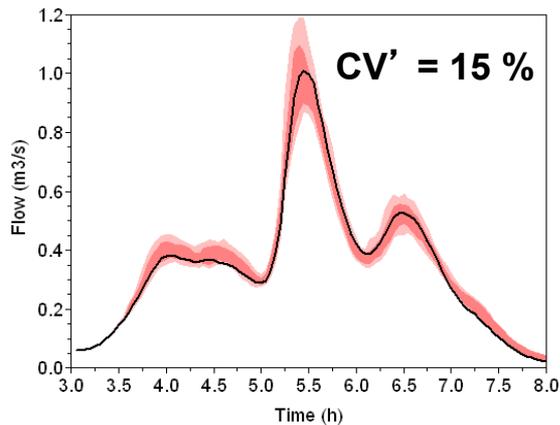
Semi-distributed 1D model



$$CV' = \frac{Q_{0.9}(t_{PF,radar}) - Q_{0.1}(t_{PF,radar})}{2 * PF_{radar}}$$

# Quantifying the uncertainty associated with small scale rainfall variability

## Upstream / downstream influence





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## Conclusion

### Quantifying the uncertainty associated with unmeasured small scale rainfall variability :

- It cannot be neglected ( $CV'$  reaches 60% for up-stream links and 15% for the outlet, and power law fall-off for probability distribution for both discharge and rainfall).
- A need to implement X band-radars (which provide an hectometric resolution) in urban area

### Comparison of a fully distributed model (10 m resolution) with semi-distributed one (300 m resolution)

- Much more uncertainty is unveiled with the fully distributed / Even moderate rainfalls are affected.
- Semi-distributed models would be unable to take advantage of an improved data resolution.

→ Small scale phenomenon must be taken into account in urban hydrology

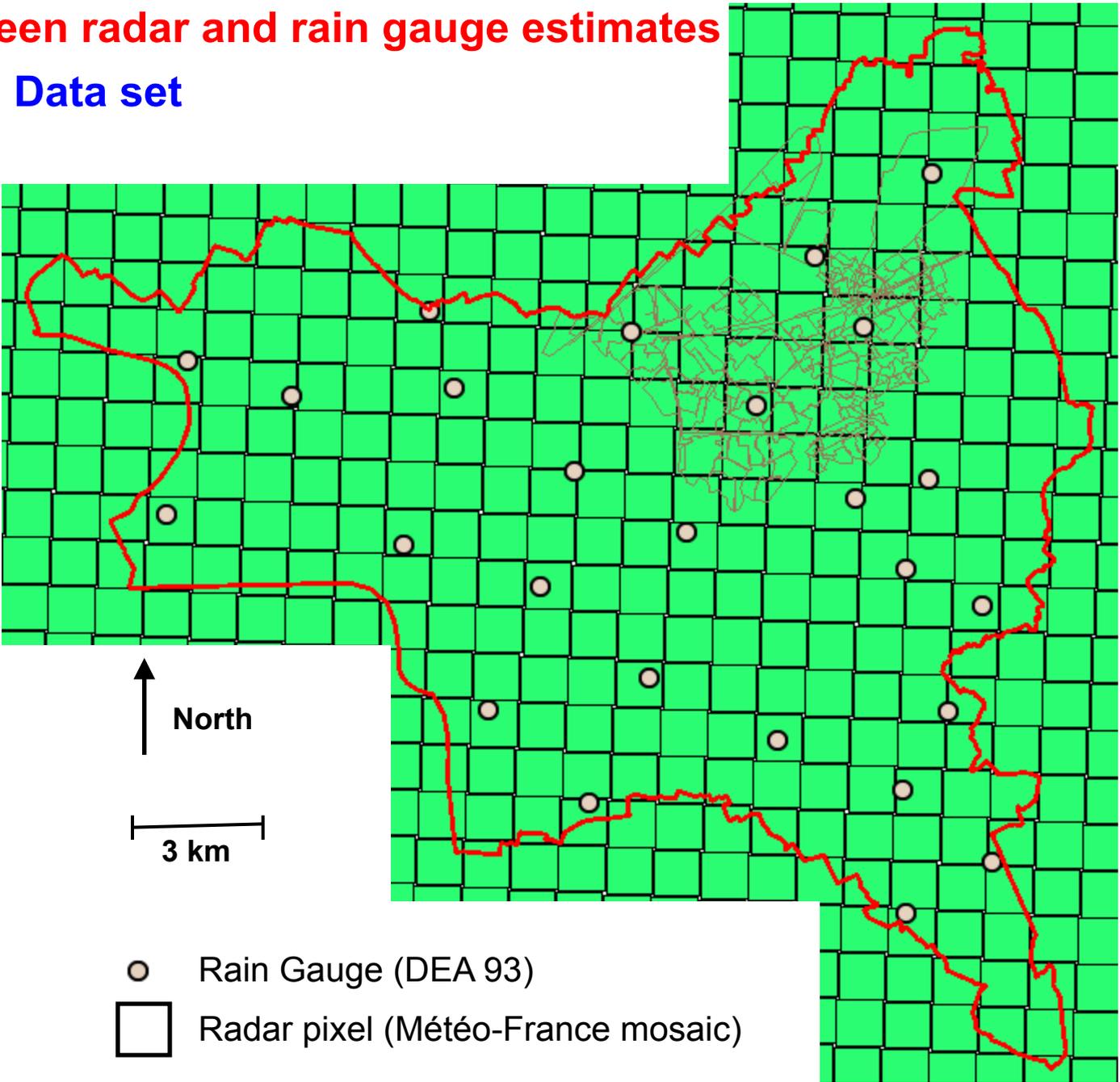
### Limits / further investigations :

- Perform similar study with other inputs
- More heaviest rainfall, actually generating floods should be tested



# Comparison between radar and rain gauge estimates

## Data set



# Comparison between radar and rain gauge estimates

- 7 steps of spatio-temporal downscaling : 1km x 5 min  $\rightarrow$  46 cm x 2.3 s
- $3^7 \times 3^7$  virtual rain gauges  $\rightarrow$  10, 25, 75 and 90 % quantile

